Summer 2019 Packet AS Math

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Rationalize the denominator.

1) $\frac{\sqrt{25}}{\sqrt{11}}$	1)	
\sim 11		
2) $\frac{5}{2}$	2)	
8 - 12		
Find the product.		
3) $(6x + 5)(3x - 8)$	3)	
Rationalize the denominator		
$4) \frac{7}{2}$	4)	
$\frac{1}{8} - \sqrt{6}$	· · · · · · · · · · · · · · · · · · ·	
Find the product		
5) $(x + 10)(x^2 + 6x - 7)$	5)	
6) $(8x^3 + 3)(x^2 + 8)$	6)	
7) Write a polynomial in standard form that represents the area of the shaded region.	7)	
	·	
x + 7		



Find the product.

8) $(5x^2 + 12x)(5x^2 - 12x)$

Perform the indicated operations.

10) $(12x^4y^2 - 6x^2y^2 + 7xy) + (9x^4y^2 - 11x^2y^2 + 4xy)$

Find the product.

8) _____

9) _____

10)

12) (7xy ² - 13y)(7xy ² + 13y)	12)
13) (p - q)(p ² + pq + q ²)	13)
Factor out the greatest common factor. 14) $14y4 = 4y3 + 8y2$	14)
Factor the trinomial, or state that the trinomial is prime	14)
15) $x^2 - x - 48$	15)
16) 2x ² - 17x + 35	16)
17) $12x^2 + 17x + 6$	17)
18) $6x^2 + 7xy + y^2$	18)
Factor the difference of two squares. 19) $25x^2 - 36y^2$	19)
20) (81x ⁴ - 1)	20)
Factor using the formula for the sum or difference of two cubes.	,
21) $x^3 + 8$	21)
22) 8x ³ - 125	22)
Factor completely, or state that the polynomial is prime. 23) 8x ⁴ - 8	23)
24) 5x ² - 5x - 30	24)
25) 108y ⁴ - 75y ²	25)
26) $2x^3 - 98a^2x + 8x^2 + 8x$	26)

3

Factor by grouping. Assume any variable exponents represent whole numbers. 30) x³ + 7x - 3x² - 21 30)

Simplify the rational expression. Find all numbers that must be excluded from the domain of the simplified rational expression.

31) $\frac{x^2 + 11x + 28}{x^2 + 14x + 49}$	31)

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- 29) Find the formula for the volume of the region outside the smaller rectangular solid and insice 29) larger rectangular solid. Express the volume in factored form.
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28)

27)

Solve the problem. 27) Write an expression for the area of the shaded region and express it in factored form. Multiply or divide as indicated.

$$32) \frac{x^2 + 9x + 20}{x^2 + x - 20} \cdot \frac{x^2 - 25}{x^2 - x - 20}$$

33)
$$\frac{x^2 + 12x + 35}{x^2 + 14x + 45} \cdot \frac{x^2 + 18x + 81}{x^2 + 16x + 63}$$
33)

$$34) \frac{(x+5)^2}{x-5} \div \frac{x^2-25}{5x-25}$$

35)
$$\frac{x^2 + 9x + 14}{x^2 + 15x + 56} \div \frac{x^2 + 2x}{x^2 + 5x - 24}$$
 35) _____

Add or subtract as indicated.

$$36) \frac{5}{x+2} - \frac{3}{x-2}$$

$$37) \frac{2}{x^2 - 3x + 2} + \frac{7}{x^2 - 1}$$

$$38) \frac{x-6}{x^2+4x-5} + \frac{2x-3}{x^2+2x-15}$$

$$38) ____$$

39) Express the perimeter of the square as a single rational expression.



40) Express the perimeter of the trapezoid as a single rational expression.

40)

36)

37)



Simplify the complex rational expression.

v

$$41) \frac{x - \frac{x}{x - 2}}{x - 3}$$

$$41) \frac{x}{-\frac{x}{x - 3}}$$

$$41) \frac{1}{-\frac{x}{x - 3}}$$

$$41) \frac{1}{-\frac{x}{x - 3}}$$

$$42) \frac{1}{-\frac{27}{x^2 - 36} + 1}$$

$$43) \frac{\frac{36y^2 - 16x^2}{xy}}{\frac{6}{x} - \frac{4}{y}}$$

$$43) \frac{1}{-\frac{6}{x} - \frac{4}{y}}$$

$$43) \frac{1}{-\frac{1}{x - 4} + 1}$$

$$44) \frac{1}{-\frac{1}{x - 4} + 1}$$

Rationalize the numerator. $\Box = \overline{\Box}$

46)
$$\frac{\sqrt{x} - \sqrt{y}}{x^2 - y^2}$$
 46) _____

Solve the linear equation.

47) 8y + 4(6 + y) = 3(y - 1) + 10y

$$48) \frac{x}{16} + \frac{9}{8} = \frac{x+3}{8}$$

$$49) \frac{x-6}{-3} + \frac{x+9}{9} = x+4$$

First, write the value or values of the variable that make a denominator zero. Then solve the equation.

50) $\frac{7}{x-4} + 1 = \frac{3}{x-4}$	50)
X - 4 X - 4	

51)
$$\frac{5}{x+1} + \frac{2}{x-1} = \frac{4}{(x+1)(x-1)}$$
 51) ____

Solve the rational equation.

52)
$$\frac{2}{x-7} + \frac{7}{7-x} = \frac{8}{x+3}$$
 52) _____

Solve the problem.

53) The formula C = $\frac{21,000 + 220x}{x}$ models the average cost per unit, C, for Electrostuff to 53)

manufacture x units of Electrogadget IV. How many units must the company produce to have an average cost per unit of \$390?

Solve the formula for the specified variable.

54)
$$A = \frac{1}{2}h(a + b)$$
 for a
 54)

 55) $A = P(1 + nr)$ for n
 55)

 56) $A = \frac{1}{2}h(B + b)$ for B
 56)

Solve the absolute value equation or indicate that the equation has no solution.

	57) $\left 4 - \frac{11}{6} x \right = 12$	57)
	58) $\left 1 - \frac{3}{4}x \right + 2 = 4$	58)
Solve	the equation by factoring. 59) $3x^2 - 8x = 0$	59)
	$60) -6x - 2 = (3x + 1)^2$	60)
Solve	the quadratic equation by the square root property. 61) $3(x - 2)^2 = 15$	61)
	62) $(3x - 5)^2 = 8$	62)
Solve	the quadratic equation by completing the square. 63) $x^2 + 8x - 3 = 0$	63)
	64) $x^2 + 3x - 9 = 0$	64)
Solve	the quadratic equation using the quadratic formula. 65) $3x^2 + x - 1 = 0$	65)
	66) $3x^2 = -12x - 2$	66)

Compute the discriminant. Then determine the number and type of solutions for the given equation.

67) $x^2 - 2x + 1 = 0$ 67) 68) $5x^2 = 4x - 2$ 68) Solve the radical equation, and check all proposed solutions. 69) 69) $\sqrt{20x - 20} = x + 4$ 70) x - $\sqrt{3x - 2} = 4$ 70) _____ 71) $\sqrt{2x}$ + 10 = x + 6 71) _____

Solve the linear inequality. Other than ϕ , use interval notation to express the solution set and graph the solution set on a number line.

$72) \frac{x}{5} - \frac{1}{6} \le \frac{x}{2} + 2$	72)
-40 -32 -24 -16 -8 0 8 16 24 32 40	
73) $-4(2x + 1) \ge 2[4x - 3(x - 1)]$	73)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
 Solve the problem. 74) It takes 18 minutes to set up a candy making machine. Once the machine is set up, it produces 20 candies per minute. Use an inequality to find the number of candies that can be produced in 7 hours if the machine has not yet been set up. 	74)
75) Claire has received scores of 85, 88, 87, and 95 on her algebra tests. What score must she receive on the fifth test to have an overall test score average of at least 90?	75)
Solve the compound inequality. Other than \emptyset , use interval notation to express the solution set and on a number line.	graph the solution set
76) $10 \le 4x - 2 \le 18$	76)

^								1.5

77) $-7 \le -2x + 5 \le 1$

Begin by graphing the standard square root function $f(x) = \sqrt{x}$. Then use transformations of this graph to graph the given function.



Begin by graphing the standard function $f(x) = x^3$ Then use transformations of this graph to graph the given function.



Begin by graphing the standard quadratic function $f(x) = x^2$. Then use transformations of this graph to graph the given function.

80)
$$g(x) = -\frac{1}{2}(x+7)^2 - 2$$
 80)



Begin by graphing the standard absolute value function f(x) = |x|. Then use transformations of this graph to graph the given function.

81) g(x) = $\frac{1}{4} x - 6 + 3$	81)
7	



Given functions f and g, perform the indicated operations.

82)
$$f(x) = \sqrt{4x + 2}$$
, $g(x) = \sqrt{25x - 16}$
Find fg. 82)

84)

85)

86)

87) _____

88)

Given functions f and g, determine the domain of f + g.

83)
$$f(x) = 2x + 1$$
, $g(x) = \frac{2}{x + 4}$ 83) _____

Find the domain of the indicated combined function.

84) Find the domain of (f + g)(x) when f(x) = 9 - 2x and g(x) = -7x + 9.

For the given functions f and g , find the indicated composition.

85) $f(x) = \frac{4}{x+6}$	$g(x) = \frac{7}{8x}$		
(f @)(x)			

86) $f(x) = 4x^2 + 2x + 5$, g(x) = 2x - 4(g f)(x)

Find the domain of the composite function f.g.

87)
$$f(x) = x + 4$$
, $g(x) = \frac{5}{x + 6}$

88)
$$f(x) = \sqrt{x};$$
 $g(x) = 5x + 25$

Find functions f and g so that $h(x) = (f \circ g)(x)$.

89)
$$h(x) = \frac{9}{x^2} + 1$$
 89) _____

90)
$$h(x) = (6x - 14)^8$$
 90)

Find the domain of the indicated combined function. 91) Find the domain of (fg)(x) when $f(x) = \sqrt{6x + 5}$ and $g(x) = \sqrt{5x - 4}$.	91)
Find the inverse of the one-to-one function.	
92) $f(x) = \frac{5}{7x - 8}$	92)
93) $f(x) = \sqrt{x + 8}$	93)
94) $f(x) = \sqrt[3]{x - 6}$	94)

Graph f as a solid line and f^{-1} as a dashed line in the same rectangular coordinate space. Use interval notation to give the domain and range of f and f^{-1} .

95)
$$f(x) = x^2 - 6, x \ge 0$$
 95)

96) $f(x) = (x - 4)^2, x \ge 4$



Use the Intermediate Value Theorem to determine whether the polynomial function has a real zero between the given integers.



11

-4 -2 -2 4 -4 -4

-6

6 x

Find a rational zero of the polynomial function and use it to find all the zeros of the function.102) $f(x) = x^3 - 8x^2 + 16x - 8$ 102)103) $f(x) = 2x^4 - 17x^3 + 59x^2 - 83x + 39$ 103)Solve the polynomial equation. In order to obtain the first root, use synthetic division to test the possible rational roots.104) $x^3 + 7x^2 + 19x + 13 = 0$ 104)105) $2x^4 - 19x^3 + 74x^2 - 127x + 78 = 0$ 105)

Graph the rational function.



107)



Find the indicated intercept(s) of the graph of the function. (y_1, y_2)

110) x-intercepts of f(x) =
$$\frac{(x-8)(2x+9)}{x^2+3x-6}$$

111) x-intercepts of f(x) =
$$\frac{x+7}{x^2+5x-3}$$

109) _____

110) _____

111) _____





114) y = 3 sin 3x



113)

114)



116) y = $3 \cos 2\pi x$





116) _____

117) _____



Use a vertical shift to graph the function.



Use a right triangle to write the expression as an algebraic expression. Assume that x is positive and in the domain of the given inverse trigonometric function.

121) sin(tan-1 x)

121) _____

118) _____

119)

122) cos(tan ⁻¹ x)	122)
123) cos(sin ⁻¹ x)	123)

124)
$$\sin(\sec^{-1}\frac{\sqrt{x^2+9}}{x})$$
 124) _____

Solve the system by the method of your choice. Identify systems with no solution and systems with infinitely many solutions, using set notation to express their solution sets.

125) $2x + y = 7$	125)
$\delta \mathbf{X} + 4\mathbf{y} = \mathbf{z} \mathbf{\delta}$	
126) $4x - 3y = 6$	126)
-12x + 9y = -24	
127) $y = 2x + 1$	127)
6x - 3y = -3	
Solve the system of equations.	
128) $x + y + z = -5$	128)
x - y + 3z = -15	
3x + 3y + 3z = -9	
129) 14 + 2z = $2(x - 3y)$	129)
4(x - 3y - z) = 28	
3(2x + y) + 4z = -22	
Find the indicated sum.	
130) Find the sum of the first 40 terms of the arithmetic sequence: -19, -23, -27, -31,	130)
131) Find the sum of the odd integers between 152 and 58.	131)
Solve the problem.	
132) A brick staircase has a total of 17 steps The bottom step requires 116 bricks. Each successive	132)
step requires 5 fewer bricks than the prior one. How many bricks are required to build the staircase?	·
133) A new exhibit is scheduled to open at the local museum. Museum officials expect that 7000	133)
people will visit the exhibit in its first week, and that the number of visitors will drop by 30	
people per week after the first week during the first 6 months. Find the total number of visitors expected in the exhibit's first 7 weeks.	

 134) A hockey player signs a contract with a starting salary of \$810,000 per year and an annual increase of 6.5% beginning in the second year. What will the athlete's salary be, to the nearest dollar, in the eighth year?
 134)

135) A pendulum bob swings through an arc 60 inches long on its first swing. Each swing thereafter, it swings only 89% as far as on the previous swing. What is the length of the arc after 12 swings? Round to two decimal places.	135)
Use the formula for the sum of the first n terms of a geometric sequence to solve. 136) Find the sum of the first 13 terms of the geometric sequence: 7, -14, 28, -56, 112,	136)
137) Find the sum of the first 11 terms of the geometric sequence: $\frac{1}{3}$, - 1, 3, - 9, 27,	137)
Solve the problem. 138) As Sunee improves her algebra skills, she takes 0.9 times as long to complete each	138)
homework assignment as she took to complete the preceeding assignment. If it took her 50 minutes to complete her first assignment, find how long it took her to complete the fifth assignment. Find the total time she took to complete her first five homework assignments. (Round to the nearest minute.)	, <u> </u>
Use the Binomial Theorem to expand the binomial and express the result in simplified form.	100)
139) $(5x + 4)^4$	139)
140) (5x - 5y) ³	140)
141) (2x - 1) ⁵	141)
142) (x ² - 2y) ⁴	142)
143) (x + 3y)6	143)
Write the first three terms in the binomial expansion, expressing the result in simplified form. 144) ($x - 4$) ¹⁷	144)
145) (2 x + 3 y) ⁷	145)
Find the term indicated in the expansion.	
146) (2x - 3y) ¹⁰ ; 4th term	146)
147) (x + 2y) ¹² ; 10th term	147)
148) (2x + 4) ⁵ ; 5th term	148)
149) $(x^2 + y^4)^9$; 6th term	149)

Solve the problem. 150) In how many ways can 5 players be assigned to 5 positions on a baseball team, assuming	150)
that any player can play any position?	
151) A restaurant offers a choice of 5 salads, 6 main courses, and 2 desserts. How many possible 3-course meals are there?	151)
152) A student must choose 1 of 5 science electives, 1 of 5 social studies electives, and 1 of 7 language electives. How many possible course selections are there?	152)
153) How many 3-letter codes can be formed using the letters A, B, C, D, and E? No letter can be used more than once.	153)
154) How many 4-digit numbers can be formed using the digits 1, 2, 3, 4, 5, 6, 7, 8, 9, and 0? No digit can be used more than once.	154)
155) A combination lock has 20 numbers on it. How many different 3-digit lock combinations are possible if no digit can be repeated?	155)
156) A church has 9 bells in its bell tower. Before each church service 4 bells are rung in sequence. No bell is rung more than once. How many sequences are there?	156)
Does the problem involve permutations or combinations? Do not solve. 157) The matching section of an exam has 3 questions and 9 possible answers. In how many different ways can a student answer the 3 questions, if none of the answer choices can be repeated?	157)
158) A club elects a president, vice-president, and secretary-treasurer. How many sets of officers are possible if there are 15 members and any member can be elected to each position? No person can hold more than one office.	158)
Solve the problem. 159) A stack of 7 different cards are shuffled and spread out face down. If 4 cards are turned face up, how many different 4-card combinations are possible?	159)
160) From 8 names on a ballot, a committee of 3 will be elected to attend a political national convention. How many different committees are possible?	160)
161) Ron finds 9 books at a bookstore that he would like to buy, but he can afford only 5 of them. In how many ways can he make his selection? How many ways can he make his	161)
selection if he decides that one of the books is a must?	

Solve the problem. Round to the nearest hundredth of a percent if needed.

162) Use of the internet for shopping is increasing dramatically, but still is somewhat age dependent. When a popular web site that sells books asked the age of users who bought products from them over the internet, they obtained the following data. What is the probability that a buyer on this web site is aged 60-69?

Age Group	Number
10-19	1962
20-29	3985
30-39	2829
40-49	635
50-59	443
60-69	308
70-79	72

163) Measurements of the height of a group of men entering a particular college produced the following table. What is the probability that a man entering the college is 68-69 inches tall?

Height (inches)	60-61	62-63	64-65	66-67	68-69	70-71	72-73	74-75	76+
Number	5	11	80	247	290	155	110	35	3

164) The table below represents the number of deaths per 100 cases for an illness having a median mortality of four years and a right-skewed distribution over time. What is the probability of living more than 12 years after diagnosis of the disease? Years after Diagnosis Number deaths

1-2	15
3-4	35
5-6	16
7-8	9
9-10	6
11-12	4
13-14	2
15+	13

Find the probability.

 169) What is the probability that a card drawn from a deck of 52 cards is not a spade?
 169)

170) A bag contains 26 marbles, of which 4 are blue and 6 are green. One marble is drawn from the bag. What is the probability that the marble drawn is not blue?

163)

164)

170)

171) Give the probability that the roll of a die will show a number less than 6.	171)
172) What is the probability that the arrow will land on an odd number?	172)
173) One digit from the number 3,151,221 is written on each of seven cards. What is the probability of drawing a card that shows 3, 1, or 5?	173)
174) A card is drawn from a deck of 52 cards. What is the probability that it is a numbered card (2-10) or a spade?	174)
175) Given the sequence 5, 6, 7, 8 42, what is the probability that a number in the sequence is odd or that it is greater than 12 and less then 27?	175)
176) A 6-sided die is rolled. What is the probability of rolling a number that is even and a 3?	176)
177) A card is drawn from a well-shuffled deck of 52 cards. What is the probability of getting a red 2?	177)
178) Urn A has balls numbered 1 through 7. Urn B has balls numbered 1 through 5. What is the probability that a 4 is drawn from A followed by a 2 from B?	178)
179) A game spinner has regions that are numbered 1 through 9. If the spinner is used twice, what is the probability that the first number is a 3 and the second is a 6?	179)
Find the derivative of f at x. That is, find $f'(x)$.	
180) $f(x) = x^2 - 8x - 11; x = 6$	180)
181) $f(x) = \sqrt{x}; x = 100$	181)
182) $f(x) = \frac{-4}{x}; x = 4$	182)
Solve the problem.	
183) The function f(x) = x ³ describes the volume of a cube, f(x), in cubic inches, whose length, width, and height each measure x inches. If x is changing, find the average rate of change of the volume with respect to x as x changes from 1 inches to 1.1 inches.	183)
184) A foul tip of a baseball is hit straight upward from a height of 4 feet with an initial velocity of 96 feet per second. The function s(t) = -16t ² + 96t describes the ball's height above the ground, s(t), in feet, t seconds after it was hit. What is the instantaneous velocity of the ball	184)

Complete the identity.	
185) $\sec x - \frac{1}{\sec x} = ?$	185)
186) $\csc x(\sin x + \cos x) = ?$	186)
187) $\frac{(\sin x + \cos x)^2}{1 + 2 \sin x \cos x} = ?$	187)
188) 2 tan x - (1 + tan x) ² = ?	188)
189) tan x(cot x - cos x) = ?	189)
190) $\sin^2 x + \sin^2 x \cot^2 x = ?$	190)
191) $\sin^2 x + \tan^2 x + \cot^2 x = ?$	191)
$192) \frac{\csc x \cot x}{\sec x} = ?$	192)
193) $\sec^4 x + \sec^2 x \tan^2 x - 2 \tan^4 x = ?$	193)
194) $\tan x \cdot \cot x = ?$	194)
195) $\frac{(\tan x + 1)(\tan x + 1) - \sec^2 x}{\tan x} = ?$	195)
196) $\frac{\cos x - \sin x}{\cos x} + \frac{\sin x - \cos x}{\sin x} = ?$	196)
197) $\frac{\cos^2 x - \sin^2 x}{1 - \tan^2 x} = ?$	197)
198) $\frac{\sin x + \cos x}{\sin x} - \frac{\cos x - \sin x}{\cos x} = ?$	198)
199) $\sin^4 x - \cos^4 x = ?$	199)
200) $\frac{(\csc x + 1)(\csc x - 1)}{\cot^2 x} = ?$	200)
201) $\cot^2 2x + \cos^2 2x + \sin^2 2x = ?$	201)

202) 1 - $\frac{\sin^2 x}{1 + \cos x} = ?$	202)
203) $\csc^2 x \sec x = ?$	203)
Verify the identity. 204) $\cot \theta \cdot \sec \theta = \csc \theta$	204)
205) $\tan \theta \cdot \csc \theta = \sec \theta$	205)
206) $\csc^2 u - \cos u \sec u = \cot^2 u$	206)
207) $(1 + \tan^2 u)(1 - \sin^2 u) = 1$	207)
208) csc u - sin u = cos u cot u	208)
209) 1 + $\sec^2 x \sin^2 x = \sec^2 x$	209)
210) $\cot^2 x + \csc^2 x = 2 \csc^2 x - 1$	210)